# Potential Energy Surfaces for the $S_{1}-S_{0}$ Relaxation of trans-Diphenyldiphosphene in the $\mathbf{P}=\mathbf{P}$ Rotation-Restricted Condition 

Yoshiaki Amatatsu ${ }^{\dagger}$<br>Faculty of Engineering and Resource Science, Akita University, Tegata Gakuen-cho, Akita 010-8502, Japan

Received: March 12, 2009; Revised Manuscript Received: June 12, 2009


#### Abstract

The potential energy surfaces (PESs) for the $\mathrm{S}_{1}-\mathrm{S}_{0}$ relaxation of trans-diphenyldiphosphene (DPP) in the $\mathrm{P}=\mathrm{P}$ rotation-restricted condition have been calculated by means of ab initio complete active space selfconsistent field and its second-order perturbation methods. Two types of PESs for the $S_{1}-S_{0}$ relaxation under $\mathrm{P}=\mathrm{P}$ rotation-restricted condition have been scanned, starting from the stable geometry in $\mathrm{S}_{1}$ where the two phenyl groups are perpendicularly twisted against the $\mathrm{P}=\mathrm{P}$ part. The nonsymmetric inversion route where one of the CPP parts takes a linear geometry is favorable. On the other hand, the symmetric inversion route where both the $\angle$ CPP angles increase simultaneously is energetically unfavorable. This is contrastive with the case of azobenzene (AZB) in the $\mathrm{N}=\mathrm{N}$ rotation-restricted condition. It has been confirmed that the discussion for the photochemistry of DPP is also true for a realistic diphosphene protected by a bulky substituent. The electronic factors on the shapes of PESs for the nonsymmetric inversion and the symmetric inversion routes of DPP have been analyzed and compared with those of AZB.


## 1. Introduction

Multiple bond compounds of heavier main group elements have been of great interest in the basic chemistry as well as the material science. ${ }^{1-3}$ For the last several years, especially, this class of compounds has been intended to be utilized as photofunctional materials. ${ }^{4-6}$ The idea of the applications to new photofunctional materials is based on the small HOMO-LUMO energy gaps of multiple bond compounds, which make it possible to tune the absorption and emission properties. In order to exploit excellent photofunctional materials, a further characterization of the excited states is desirable, although the $\mathrm{P}=\mathrm{P}$ bonding nature in the ground state has been studied. ${ }^{7}$ Very recently we gave a new insight about the excited states of diphenyldiphosphene ( $\mathrm{PhP}=\mathrm{PPh}, \mathrm{Ph}$, phenyl group) (denoted by DPP hereafter) which is an analogue of azobenzene $(\mathrm{PhN}=\mathrm{NPh})\left(\right.$ denoted by AZB). ${ }^{8}$ Though the electronic structures of DPP are similar to those of AZB, the potential energy surface (PES) in $\mathrm{S}_{1}$ with respect to the phenyl torsions is quite different from that of AZB. At the stable geometry of DPP in $S_{1}$ around the Franck-Condon region (denoted by $\mathrm{S}_{1}$-geometry(90)), two phenyl groups of DPP are perpendicularly twisted against the $\mathrm{P}=\mathrm{P}$ part (i.e., $\phi \sim \phi^{\prime} \sim 90^{\circ}$ and $\tau \sim 180^{\circ}$ in Figure $1)$. At the stable geometry of AZB in $S_{1}\left(S_{1}\right.$-geometry $\left(C_{2 h}\right)$ ), on the other hand, AZB takes a planar structure with $C_{2 h}$ symmetry (i.e., $\phi=\phi^{\prime}=0^{\circ}$ and $\tau=180^{\circ}$ ). This implies that the photochemical behavior of DPP is different from that of AZB. In the present paper, we focus our interest on the $S_{1}-S_{0}$ relaxation process of DPP where the $\mathrm{P}=\mathrm{P}$ rotation is restricted spatially, in comparison with that of AZB.

The $S_{1}-S_{0}$ relaxation process of AZB has been extensively studied experimentally ${ }^{9-24}$ as well as theoretically, ${ }^{25-30}$ although it is still controversial. A common feature of the photochemical behavior upon $\mathrm{S}_{1}$ excitation is that the quantum yield is almost constant ( $\sim 0.25$ ) independent of the surroundings. ${ }^{9,10}$ Contrary to the independence of the quantum yield on the surroundings, the lifetime in $S_{1}$ is strongly dependent on them. In $n$-hexane,

[^0]

Figure 1. Numbering of atoms in DPP. The bending angles of $\angle C^{1} \mathrm{P}^{\alpha} \mathrm{P}^{\beta}$ and $\angle \mathrm{C}^{1^{\prime}} \mathrm{P}^{\beta} \mathrm{P}^{\alpha}$ are denoted by $\alpha$ and $\beta$. The dihedral angles of $\angle \mathrm{C}^{1} \mathrm{P}^{\alpha} \mathrm{P}^{\beta} \mathrm{C}^{1^{\prime}}, \angle \mathrm{C}^{2} \mathrm{C}^{1} \mathrm{P}^{\alpha} \mathrm{P}^{\beta}$, and $\angle \mathrm{P}^{\alpha} \mathrm{P}^{\beta} \mathrm{C}^{1^{\prime}} \mathrm{C}^{2^{\prime}}$ are denoted by $\tau$, $\phi$, and $\phi^{\prime}$. The similar definitions of the numbering of atoms and the internal coordinates in AZB are made.
the fluorescence exhibits biphasic decay;; ${ }^{12,13,16,18,19,22,23}$ the time constants for the shorter and longer components are 0.34 and 3.0 ps , respectively. ${ }^{18}$ The biphasic decays are also found in the photochemistry of substituted azobenzenes. ${ }^{11,17,20,24}$ In case that the $\mathrm{N}=\mathrm{N}$ rotation is restricted in viscous solvent of ethylene glycol, within a cyclodextrin cavity, or with a chemical modification by cyclophane or crown ether, it also exhibits biphasic decay, but the longer time constant is much larger. ${ }^{14,15,22,23}$ In order to explain the lifetime dependent on the surroundings, it is proposed that AZB in $S_{1}$ takes different routes for the relaxation into $\mathrm{S}_{0}$. In the former case (i.e., $n$-hexane) which allows the $\mathrm{N}=\mathrm{N}$ rotation, AZB in $\mathrm{S}_{1}$ takes a "rotation" route by twisting the $\mathrm{N}=\mathrm{N}$ bond for the relaxation into $\mathrm{S}_{0}$. The temporal behavior of the fluorescence depolarization supports this route. ${ }^{21}$ In addition, the PESs by high levels of quantum mechanical calculations support the rotation route. ${ }^{25-29}$ In the latter cases that the surroundings prevent the $\mathrm{N}=\mathrm{N}$ rotation, there are two possible $S_{1}-S_{0}$ relaxation routes of AZB, schematically shown in Figure 2. One candidate is "nonsymmetric inversion" route where the inversion about one N atom


Figure 2. Possible routes in $S_{1}$ for the $S_{1}-S_{0}$ relaxation of AZB in the $\mathrm{N}=\mathrm{N}$ rotation-restricted condition.

## nonsymmetric inversion



Figure 3. Possible routes from the $S_{1}$-geometry(90) in $S_{1}$ for the $S_{1}-S_{0}$ relaxation of DPP in the $\mathrm{P}=\mathrm{P}$ rotation-restricted condition.
takes place in the same molecular plane. By quantum mechanical calculations, it is found that the $S_{1}$ and $S_{0}$ PESs do not cross each other in case that one of the $\angle \mathrm{CNN}$ angles is large but the other is kept small. ${ }^{26,28,29}$ Another candidate is a "symmetric inversion" route where the two $\angle \mathrm{CNN}$ angles simultaneously increase in the same molecular plane. The $\mathrm{S}_{1}$ and $\mathrm{S}_{0}$ PESs with respect to the symmetric increase of the two $\angle \mathrm{CNN}$ angles cross each other at $\angle \mathrm{CNN} \sim 157^{\circ}$ where the energy is above the stable geometry in $\mathrm{S}_{1}$ by $0.92 \mathrm{eV}(21.2 \mathrm{kcal} / \mathrm{mol}){ }^{26}$ The temporal behavior of the fluorescence depolarization modestly also supports the symmetric inversion route. ${ }^{21}$ Here we note that the "nonsymmetric inversion" and "symmetric inversion" in our present paper are referred as "inversion" and "concerted inversion" in some cases. ${ }^{21,22,26}$
Concerning the $S_{1}-S_{0}$ relaxation routes of DPP from the stable $\mathrm{S}_{1}$-geometry $(90)$ of DPP under $\mathrm{P}=\mathrm{P}$ rotation-restricted condition, there are at least two possible relaxation routes schematically shown in Figure 3. So our present concern is about the PESs along the nonsymmetric inversion and the symmetric inversion routes from the $S_{1}$-geometry (90). Thereby, we try to characterize the $\mathrm{P}=\mathrm{P}$ double bond from a viewpoint of the excited state, in comparison with the $\mathrm{N}=\mathrm{N}$ double bond of AZB.

The present paper is organized as follows. In the next section, we describe the computational strategy for the present calculation. In section 3, we discuss the PESs of DPP and AZB along the nonsymmetric inversion and the symmetric inversion routes. Then we examine the electronic effects on the shapes of the PESs so as to extract the characteristics of the $\mathrm{P}=\mathrm{P}$ double bond. Furthermore, we make comment on the $\mathrm{S}_{1}-\mathrm{S}_{0}$ relaxation process of realistic diphosphenes protected by a bulky substituent. Last of all, we give a summary on the present computational results and future perspective of the photochemistry of diphosphenes.

## 2. Method of Calculations

In the present calculations, we took a computational strategy the same as our previous one. ${ }^{8}$ A complete active space self-
consistent field (CASSCF) calculation where all the nine $\pi$-type occupied orbitals (including two nonbonding orbitals on the P atoms) and the lowest seven unoccupied $\pi^{*}$ orbitals are taken into account (denoted by $(18,16) \mathrm{CASSCF}$ ) is desirable but impractical to scan the global PESs for the $\mathrm{S}_{1}-\mathrm{S}_{0}$ relaxation process of DPP. So we preliminarily performed configuration interaction (CI) calculations where up to triple excitations from the Hartree-Fock configuration were taken into account. Thereby, it is found that at most the highest five $\pi$ occupied and the lowest five $\pi^{*}$ unoccupied orbitals as well as two nonbonding orbitals on the P atoms are enough to describe our present interest of $S_{0}$ and $S_{1}$ states at any geometries which possibly contribute to the photochemistry of DPP. So we adopted 14 electrons in 12 orbitals CASSCF $((14,12)$ CASSCF $)$ for scanning of the global PESs. In necessity, we made correction for $(14,12)$ CASSCF energy of each electronic state using the second-order multireference Möller-Plesset perturbation (MRMP2) method where all valence and virtual orbitals were included.

First we scanned the PESs of the nonsymmetric inversion and the symmetric inversion routes (see Figure 3). As mentioned later, the nonsymmetric inversion route is more realistic in the $\mathrm{S}_{1}-\mathrm{S}_{0}$ relaxation of DPP under constraint that the $\mathrm{P}=\mathrm{P}$ rotation is restricted spatially. Then we determined the conical intersection between $\mathrm{S}_{1}$ and $\mathrm{S}_{0}\left(\mathrm{~S}_{1} / \mathrm{S}_{0}-\mathrm{CIX}\right)$ to examine the inversion route in detail. Here we determined the $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX by a smaller $(8,5)$ CASSCF method because the $S_{1} / S_{0}$-CIX region is well described by the four highest occupied MOs (HOMOs) and the lowest unoccupied MO (LUMO). After the determination of $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX by $(8,5) \mathrm{CASSCF}$, however, we performed the present standard $(14,12)$ CASSCF calculation at the $S_{1} / S_{0}$-CIX to verify that the energy difference between $S_{1}$ and $S_{0}$ is small enough to be a CIX. This implies that a much more computationally demanding $(14,12)$ CASSCF gives an $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX similar to that by $(8,5)$ CASSCF.

Then we also did similar calculations (i.e., scanning of the PESs for the $S_{1}-S_{0}$ relaxation routes in Figure 2) of AZB by $(14,12)$ CASSCF and MRMP2 methods. Thereby, we compare the photochemistry of DPP with that of AZB under $N=N$ rotation-restricted condition.

In order to confirm that the discussion on the photochemistry of DPP is valid for a realistic diphosphene of which the $\mathrm{P}=\mathrm{P}$ part is protected by a bulky substituent, we performed similar calculations of bis(2,6-dimethylphenyl)diphosphene by $(14,12)$ CASSCF and MRMP2 methods.

In the scanning of the PESs, we used the GAMESS program in the present ab initio calculations with the Huzinaga-Dunning double- $\zeta$ basis set augmented by polarizations ( $\alpha_{d}=0.75$ for C atoms, $\alpha_{\mathrm{d}}=0.55$ for P atoms, and $\alpha_{\mathrm{d}}=0.80$ for N atoms). ${ }^{31}$ In the determination of the $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX for the inversion route of DPP, we used Gaussian03 with a smaller basis set where the polarization function is augmented only on the P atoms. ${ }^{32}$

## 3. Results and Discussion

3.1. $\mathbf{S}_{\mathbf{1}}-\mathbf{S}_{\mathbf{0}}$ Relaxation Routes of DPP. Figure 4 a shows the PESs of the nonsymmetric inversion route, which were obtained as a function of the $\angle C^{1} \mathrm{P}^{\alpha} \mathrm{P}^{\beta}$ bending angle $\alpha$ where the other parameters in $\mathrm{S}_{1}$ are optimized under constraint that DPP has $C_{s}$ symmetry and the two phenyl groups are perpendicularly twisted. In this route, the $S_{1}$ state is not so destabilized even at a large $\alpha$, while the $S_{0}$ state is destabilized so as to be close to the $S_{1}$ state. Then we calculated the PESs in the region around $\alpha=180^{\circ}$ in order to determine another important internal coordinate for the surface crossing between $S_{1}$ and $S_{0}$. Figure


Figure 4. Potential energy surfaces (PESs) for the nonsymmetric inversion route of DPP: the solid lines are for $S_{1}$, and the dotted lines are for $S_{0}$. (a) The PESs are obtained as a function of $\alpha$ where the other geometrical parameters are optimized in $\mathrm{S}_{1}$ under the constraint that DPP has $C_{s}$ symmetry and the two phenyl groups are perpendicularly twisted against the $\mathrm{P}=\mathrm{P}$ part. (b) The PESs are obtained as a function of $\beta$ where $\alpha$ is fixed to $180^{\circ}$ and the two phenyl groups are perpendicularly twisted but the remaining parameters are optimized in $S_{1}$. The energy in $S_{0}$ is evaluated at each optimized geometry in $S_{1}$. Note that the $\alpha>180^{\circ}$ of the abscissa corresponds to the cis-form region. The energy scale of the ordinate in panel $b$ is half that of panel $a$.

TABLE 1: Characteristic Optimized Parameters at Important Conformations of DPP and AZB

| DPP | $\mathrm{S}_{0}$ - geometry $^{\text {a }}$ | $\begin{aligned} & \text { S }_{1} \text {-geometry- } \\ & (90)^{a} \end{aligned}$ | $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX | $\underset{(\mathrm{sym})^{b}}{\mathrm{~S}_{1} / \mathrm{S}_{0} \text {-CIX- }}$ |
| :---: | :---: | :---: | :---: | :---: |
| Bond Distances (angstroms) |  |  |  |  |
| $\mathrm{P}^{\alpha} \mathrm{P}^{\beta}$ | 2.056 | 2.153 | 2.217 | 1.957 |
| $\mathrm{P}^{\alpha} \mathrm{C}^{1}$ | 1.834 | 1.821 | 1.817 | 1.810 |
| $\mathrm{P}^{\beta} \mathrm{C}^{1^{\prime}}$ | 1.834 | 1.821 | 1.858 | 1.810 |
| Bond Angles (deg) |  |  |  |  |
| $\alpha\left(C^{1} \mathrm{P}^{\alpha} \mathrm{P}^{\beta}\right)$ | 103.1 | 109.0 | 168.3 | 172.0 |
| $\beta\left(\mathrm{C}^{1^{\prime}} \mathrm{P}^{\beta} \mathrm{P}^{\alpha}\right)$ | 103.1 | 109.0 | 74.8 | 172.0 |
| Dihedral Angles (deg) |  |  |  |  |
| $\tau\left(\mathrm{C}^{1} \mathrm{P}^{\alpha} \mathrm{P}^{\beta} \mathrm{C}^{1}\right)$ | -177.9 | -179.1 | 0.0 | 180.0 |
| $\phi\left(\mathrm{C}^{2} \mathrm{C}^{1} \mathrm{P}^{\alpha} \mathrm{P}^{\beta}\right)$ | 30.3 | 89.6 | 90.6 | 92.2 |
| $\phi^{\prime}\left(\mathrm{C}^{2} \mathrm{C}^{1^{\prime}} \mathrm{P}^{\beta} \mathrm{P}^{\alpha}\right)$ | 30.3 | 89.6 | 92.2 | 92.2 |
| AZB | $\mathrm{S}_{0}$-geometry ${ }^{a}$ | $S_{1}$-geometry( |  | CIX (sym) ${ }^{c}$ |
| Bond Distances (angstroms) |  |  |  |  |
| $\mathrm{N}^{\alpha} \mathrm{N}^{\beta}$ | 1.246 | 1.257 |  | 1.217 |
| $\mathrm{N}^{\alpha} \mathrm{C}^{1}$ | 1.426 | 1.369 |  | 1.347 |
| $\mathrm{N}^{\beta} \mathrm{C}^{1^{\prime}}$ | 1.426 | 1.369 |  | 1.347 |
| Bond Angles (deg) |  |  |  |  |
| $\alpha\left(\mathrm{C}^{1} \mathrm{~N}^{\alpha} \mathrm{N}^{\beta}\right)$ | 114.8 | 128.4 |  | 154.5 |
| $\beta\left(\mathrm{C}^{1} \mathrm{~N}^{\beta} \mathrm{N}^{\alpha}\right)$ | 114.8 | 128.4 |  | 154.5 |
| Dihedral Angles (deg) |  |  |  |  |
| $\tau\left(\mathrm{C}^{1} \mathrm{~N}^{\alpha} \mathrm{N}^{\beta} \mathrm{C}^{1^{\prime}}\right)$ | 180.0 | 180.0 |  | 180.0 |
| $\phi\left(\mathrm{C}^{2} \mathrm{C}^{1} \mathrm{~N}^{\alpha} \mathrm{N}^{\beta}\right)$ | 0.0 | 0.0 |  | 0.0 |
| $\phi^{\prime}\left(\mathrm{C}^{2^{\prime}} \mathrm{C}^{1^{\prime}} \mathrm{N}^{\beta} \mathrm{N}^{\alpha}\right)$ | 0.0 | 0.0 |  | 0.0 |

${ }^{a}$ The values are taken from ref 8. The $\mathrm{S}_{1}$-geometry $(90)$ was referred as the $\mathrm{S}_{1}$-geometry in ref $8 .{ }^{b}$ The $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX(sym) of DPP is a crossing point for the symmetric inversion route in Figure 5. ${ }^{c}$ The $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX(sym) of AZB is a crossing point for the symmetric inversion route in Figure 7.

4 b shows the PESs as a function of the other $\angle \mathrm{C}^{1^{\prime}} \mathrm{P}^{\beta} \mathrm{P}^{\alpha}$ bending angle $\beta$ where $\alpha$ is fixed to $180^{\circ}$ and the remaining parameters are optimized in $S_{1}$. From this figure, it is found that a large $\alpha$ $\left(\sim 180^{\circ}\right)$ and a small $\beta\left(\sim 75^{\circ}\right)$ are essential to surface crossing between $S_{1}$ and $S_{0}$. Actually, the $S_{1} / S_{0}$-CIX is located in this region by means of a smaller $(8,5)$ CASSCF with a smaller basis set (refer to Table 1). We checked the energy difference between $S_{1}$ and $S_{0}$ by the present standard $(14,12)$ CASSCF method at the $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX. As seen in Table 2, the energy difference ( 0.014 $\mathrm{eV})$ is small enough to be a CIX even by $(14,12)$ CASSCF. This

## TABLE 2: Electronic Structures of DPP at $\mathbf{S}_{\mathbf{1}} / \mathbf{S}_{\mathbf{0}}$-CIX

|  | energy $(\mathrm{eV})^{a}$ | dipole moment (debye) | main CSFs $^{b}$ |
| :--- | :---: | :---: | :--- |
| $\mathrm{~S}_{0}$ | 4.816 | 1.333 | 0.885 (closed shell) |
| $\mathrm{S}_{1}$ | 4.802 | 2.049 | 0.910 (1-1') |

${ }^{a}$ The energies in $\mathrm{S}_{0}$ and $\mathrm{S}_{1}$ at $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX are not exactly same. This is because the $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX geometry is optimized by $(8,5)$ CASSCF but the energies in this table are evaluated by the present standard $(14,12)$ CASSCF. ${ }^{b}$ The CSFs (configuration state functions) of which absolute values of CI coefficients are greater than 0.3 are listed. The seven occupied $\pi$ orbitals (including two nonbonding orbitals) and the lowest five unoccupied $\pi^{*}$ ones in the order of energy are designated by $7,6,5,4,3,2,1$ (HOMO), $1^{\prime}$ (LUMO), $2^{\prime}, 3^{\prime}, 4^{\prime}, 5^{\prime}$, respectively. $1-1^{\prime}$ in the parentheses, for instance, indicates the CSF of single excitation from orbital 1 to $1^{\prime}$.
implies that an $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX by a terribly computationally demanding $(14,12)$ CASSCF is similar to the $S_{1} / S_{0}$-CIX by $(8,5)$ CASSCF with a smaller basis set.

Our next concern is how electronically excited DPP travels from $\mathrm{S}_{0}$-geometry into $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX. Although the intrinsic reaction coordinate analysis or molecular dynamics simulation is desirable to obtain detailed information, we examined it by an easier approach of two types of geometry optimizations in $S_{1}$ from $\mathrm{S}_{0}$-geometry and $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX, respectively. Both of the optimizations substantially give the stable geometry in $S_{1}$ around the Franck-Condon region (denoted by $\mathrm{S}_{1}$-geometry(90) in Table 1) where the two phenyl groups are almost perpendicularly twisted against the $\mathrm{P}=\mathrm{P}$ part. This implies that the route of $\mathrm{S}_{0^{-}}$ geometry $\rightarrow \mathrm{S}_{1}$-geometry $(90) \rightarrow \mathrm{S}_{1} / \mathrm{S}_{0}$-CIX is likely. Concerning the geometrical change of $\mathrm{S}_{0}$-geometry $\rightarrow \mathrm{S}_{1}$-geometry(90) in $S_{1}$, we can easily deduce from Table 1 and the $S_{1}$ gradients with respect to the internal coordinates. The $\mathrm{S}_{1}$ gradients of the $\mathrm{P}=\mathrm{P}$ stretch, the $\angle \mathrm{CPP}$ bending, and the phenyl torsion are large at $\mathrm{S}_{0}$-geometry $(-0.035,-0.047$, and -0.004 au , respectively). This means the initial events upon electronic excitation into $\mathrm{S}_{1}$ at the $\mathrm{S}_{0}$-geometry are the elongation of the $\mathrm{P}=\mathrm{P}$ bond, the enlargement of the $\angle \mathrm{CPP}$ angles, and the phenyl torsion toward the perpendicularly twisted conformation. In comparison of the $S_{0}$-geometry with the $S_{1}$-geometry(90) in Table 1, it is found that the initial events in $S_{1}$ directly connect the $S_{0}$-geometry with the $S_{1}$-geometry $(90)$. In the second stage of $S_{1}$-geometry $\rightarrow \mathrm{S}_{1} / \mathrm{S}_{0}$-CIX, the asymmetrization of the two $\angle \mathrm{CPP}$ angles ( $\alpha$ and $\beta$ ) is important, while the other parameters remain almost unchanged. One of the $\angle \mathrm{CPP}$ angles, $\alpha$, increases to take a linear

TABLE 3: Energies (eV) at Important Conformations of DPP and AZB

| DPP | $\mathrm{S}_{0}$-geometry ${ }^{a}$ |  |  | $\mathrm{S}_{1}$-geometry- <br> $(90)$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{S}_{0}$ | $0.0(0.0)^{b}$ |  | $\mathrm{~S}_{1} / \mathrm{S}_{0}$-CIX | $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX- <br> $(\mathrm{sym})$ |
| $\mathrm{S}_{1}$ | $3.544(2.759)$ | $3.125(2.577)$ | $4.802(4.107)$ | $7.458(6.812)$ |
| AZB | $\mathrm{S}_{0}$-geometry ${ }^{a}$ | $\mathrm{~S}_{1}$-geometry $\left(C_{2 h}\right)$ | $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX $(\mathrm{sym})$ |  |
| $\mathrm{S}_{0}$ | $0.0(0.0)$ |  |  | $3.631(3.439)$ |
| $\mathrm{S}_{1}$ | $3.277(2.412)$ | $2.718(1.888)$ | $3.629(2.807)$ |  |

${ }^{a}$ The values are taken from ref $8 .{ }^{b}$ The numbers in the parentheses are the MRMP2 values.


Figure 5. Potential energy surfaces (PESs) for the symmetric inversion route of DPP: the solid lines are for $S_{1}$, and the dotted lines are for $\mathrm{S}_{0}$. The PESs are obtained as a function of $\alpha$ where the two phenyl groups are perpendicularly twisted against the $\mathrm{P}=\mathrm{P}$ part and the other geometrical parameters are optimized in $\mathrm{S}_{1}$ under constraint of $C_{2 h}$ symmetry at the phenyl perpendicularly twisted conformation. The energy in $S_{0}$ is evaluated at the optimized geometry in $S_{1}$ for each $\alpha$.
shape of the $\mathrm{C}^{1} \mathrm{P}^{\alpha} \mathrm{P}^{\beta}$ part, while the other, $\beta$, decreases to access the $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX.

Here we briefly mention the reliability of the energies before further discussion on the PESs of the photochemical process. Table 3 lists the energies at important conformations by CASSCF and MRMP2 methods. The MRMP2 energies are lower by $0.5-0.7 \mathrm{eV}$ than the CASSCF energies irrespective of the conformations. This implies that the shapes of PESs by MRMP2 are similar to those by $(14,12)$ CASSCF. The MRMP2 energy in $S_{1}$ at $S_{0}$-geometry ( 2.759 eV ) is in good agreement with the experimental absorption maximum ( $2.695 \mathrm{eV} ; 460 \mathrm{~nm}$ ) of a realistic diphosphene protected by a bulky substituent. ${ }^{33}$ From these computational findings, our present standard $(14,12)$ CASSCF is reliable enough to discuss the photochemistry but the MRMP2 energies are proper for the comparison with the experimental values. From now on, we refer the MRMP2 values as for the energies. In the first process of $\mathrm{S}_{0}$-geometry $\rightarrow \mathrm{S}_{1}$-geometry(90), DPP in $\mathrm{S}_{1}$ is stabilized, but in the second process of $S_{1}$-geometry $(90) \rightarrow \mathrm{S}_{1} / \mathrm{S}_{0}$-CIX, DPP is much destabilized by $\sim 1.44 \mathrm{eV}$.
Figure 5 shows the PESs of the symmetric inversion route, where the two $\angle \mathrm{CPP}$ angles, $\alpha$ and $\beta$, take a same value but the other geometrical parameters are optimized under constraint of $C_{2 h}$ at the phenyl perpendicularly twisted conformations. It is found that the $\mathrm{S}_{1}$ and $\mathrm{S}_{0}$ surfaces cross at a large $\angle \mathrm{CPP}$ bending angle $\alpha=\beta \sim 172^{\circ}$, but the energy at the crossing point (i.e., $\left.\mathrm{S}_{1} / \mathrm{S}_{0}-\mathrm{CIX}(\mathrm{sym})\right)$ is much higher $(\sim 2.5 \mathrm{eV})$ than that at the $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX for the nonsymmetric inversion route. This
implies that the nonsymmetric inversion route is more realistic than that of the symmetric inversion route for the $S_{1}-S_{0}$ relaxation in the $\mathrm{P}=\mathrm{P}$ rotation-restricted condition.
3.2. $\mathbf{S}_{\mathbf{1}}-\mathbf{S}_{\mathbf{0}}$ Relaxation Routes of AZB. Though the PESs of the $S_{1}-S_{0}$ relaxation routes of AZB in the $N=N$ rotationrestricted condition have been already reported by several authors, ${ }^{26,28,29}$ we also scanned the PESs for the routes in Figure 2 in order to compare with the $S_{1}-S_{0}$ relaxation routes of DPP. The nonsymmetric inversion PESs in Figure 6a are obtained as a function of $\angle C^{1} N^{\alpha} N^{\beta}$ angle $\alpha$ where the other geometrical parameters are optimized in $\mathrm{S}_{1}$ under constraint of $C_{s}$ symmetry at $\phi=\phi^{\prime}=0.0^{\circ}$. The symmetric inversion PESs in Figure 7 is obtained by a similar way under constraint of $C_{2 h}$ symmetry. Here we note that the starting $\mathrm{S}_{0}$-geometry of AZB is planar (see the relevant part of AZB in Table 1) and that AZB in $S_{1}$ maintains a planar conformation in both cases of the symmetric and nonsymmetric inversion routes. Contrary to the case of DPP, the $\mathrm{S}_{1}$ state for the symmetric inversion route is not so destabilized even at a large $\angle \mathrm{CNN}$ angle $\alpha$, while the $\mathrm{S}_{0}$ state is quickly destabilized as increase of $\alpha$. This leads to surface crossing between $S_{1}$ and $S_{0}$ in low energy at a large $\alpha$. In the nonsymmetric inversion route, the shapes of the $S_{1}$ and $S_{0}$ PESs are similar to those of DPP in Figure 4a. So we further examined the PESs around the $\alpha=180^{\circ}$ region as a function of the other $\angle \mathrm{C}^{1^{\prime}} \mathrm{N}^{\beta} \mathrm{N}^{\alpha}$ angle $\beta$. Figure 6 b shows the PESs as a function of $\beta$ where $\alpha$ is fixed to $180^{\circ}$ and the remaining geometrical parameters are optimized in $\mathrm{S}_{1}$ under constraint of $C_{s}$ symmetry. It is found that the $S_{1}$ and $S_{0}$ PESs cross each other in a large- $\beta$ region, leading to the same crossing point for the symmetric inversion.
3.3. Electronic Factors. In the previous subsections, we found out that the nonsymmetric inversion route of DPP is favorable for the $\mathrm{S}_{1}-\mathrm{S}_{0}$ relaxation under $\mathrm{P}=\mathrm{P}$ rotation-restricted condition, whereas the symmetric inversion route is favorable in the case of AZB. So we examine the electronic factors on the shapes of the PESs for the different $S_{1}-S_{0}$ relaxation routes. Concerning the first processes (i.e., $\mathrm{S}_{0^{-}}$geometry $\rightarrow \mathrm{S}_{1^{-}}$ geometry (90) for DPP, $\mathrm{S}_{0}$-geometry $\rightarrow \mathrm{S}_{1}$-geometry $\left(C_{2 h}\right)$ for AZB) after electronic excitation into $S_{1}$, we discussed the details in our previous paper. ${ }^{8}$ However, we make a brief review on them (refer to Table 4). In the case of DPP, the electron in the 3 s and the in-plane 3 p (i.e., $3 \mathrm{p}_{x}+3 \mathrm{p}_{y}$ ) orbitals decreases from $0.937,2.116$ into $0.892,1.784$, respectively, while the electron in the out-of-plane $3 p_{z}$ increases from 0.994 into 1.397. This is ascribed to the fact that the electronic excitation into $S_{1}$ is $n-\pi^{*}$. In the process of $S_{0}$-geometry $\rightarrow S_{1}$-geometry $(90)$ in $S_{1}$, the electron in the 3 s and the in-plane 3 p orbitals on the P atoms increases into $0.915,1.802$, while that on the $3 \mathrm{p}_{z}$ orbital (1.402) little changes. As analyzed in our previous paper, the increase of the 3 s and the in-plane 3 p electron on the P atoms is due to an effective interaction of the nonbonding orbitals in the $\mathrm{P}=\mathrm{P}$ part with the $\pi$ orbitals over the phenyl groups, which leads to $\mathrm{S}_{1}$-geometry (90) where the two phenyl groups are perpendicularly twisted against the $\mathrm{P}=\mathrm{P}$ part (i.e., $\phi \sim \phi^{\prime} \sim 90^{\circ}$ ). In the case of AZB, on the other hand, the out-of-plane $2 \mathrm{p}_{z}$ electron decreases from 1.370 into 1.350 in the process of $\mathrm{S}_{0}$-geometry to $S_{1}$-geometry $\left(C_{2 h}\right)$ (refer to Table 5). This is due to the enhancement of the $\pi$ conjugation between the $N=N$ part and the phenyl groups. In other words, the $\pi$ electron over the $N=N$ part is more delocalized entirely over a molecule in $S_{1}$, which geometrically reflects shrinking of the linkage CN bonds (1.426 $\AA$ at $S_{0}$-geometry, $1.369 \AA$ at $S_{1}$-geometry $\left(C_{2 h}\right)$ ) in the AZB part of Table 1.


Figure 6. Potential energy surfaces (PESs) for the nonsymmetric inversion route of AZB: the solid lines are for $\mathrm{S}_{1}$, and the dotted lines for $\mathrm{S}_{0}$. (a) The PESs are obtained as a function of $\alpha$ where the other geometrical parameters are optimized in $\mathrm{S}_{1}$ under constraint of planar structure. (b) The PESs are obtained as a function of $\beta$ where $\alpha$ is fixed to $180^{\circ}$ but the remaining parameters are optimized in $\mathrm{S}_{1}$. The energy in $\mathrm{S}_{0}$ is evaluated at the optimized geometry in $\mathrm{S}_{1}$. Note that the $\alpha>180^{\circ}$ of the abscissa corresponds to the cis-form region.


Figure 7. Potential energy surfaces (PESs) for the symmetric inversion route of AZB: the solid lines are for $S_{1}$, and the dotted lines are for $S_{0}$. The PESs are obtained as a function of $\alpha$ where the other geometrical parameters are optimized in $S_{1}$ under constraint of $C_{2 h}$ symmetry at $\phi$ $=\phi^{\prime}=0^{\circ}$. The energy in $S_{0}$ is evaluated at the optimized geometry in $S_{1}$ for each $\alpha$.

Now we discuss the second steps starting from the stable geometries in $S_{1}$ around the Franck-Condon region (i.e., $S_{1^{-}}$ geometry (90) for DPP and $S_{1}$-geometry $\left(C_{2 h}\right)$ for AZB , respectively). In the process of $S_{1}$-geometry $(90) \rightarrow S_{1} / S_{0}$-CIX where the two $\angle \mathrm{CPP}$ angles $\alpha$ and $\beta$ are asymmetrized, the electron in the in-plane 3 p (i.e., $3 \mathrm{p}_{x}+3 \mathrm{p}_{y}$ ) orbitals on the $\mathrm{P}^{\alpha}$ atom increases from 1.802 into 1.916 , while that on the $\mathrm{P}^{\beta}$ atom decreases into 1.709 (see Table 4). The out-of-plane $3 \mathrm{p}_{z}$ electron on each P atom exhibits a same trend (i.e., increase from 1.402 into 1.584 on the $\mathrm{P}^{\alpha}$ atom, decrease from 1.402 into 1.195 on the $\mathrm{P}^{\beta}$ atom, respectively). In other words, the 3 p (i.e., $3 \mathrm{p}_{x}, 3 \mathrm{p}_{y}$, and $3 p_{z}$ ) electron over the $\mathrm{P}=\mathrm{P}$ part is populated evenly on both the $\mathrm{P}^{\alpha}$ and $\mathrm{P}^{\beta}$ atoms around the $\mathrm{S}_{1}$-geometry(90). In the asymmetrization process of $\alpha$ and $\beta$ (i.e., nonsymmetric inversion route), however, the 3 p electron turns to be populated mainly on the $\mathrm{P}^{\alpha}$ atom which relates to the larger $\angle \mathrm{CPP}$ angle. Furthermore, the sums of the in-plane 3 p (i.e., $3 p_{x}+3 p_{y}$ ) and the out-of-plane $3 p_{z}$ electron on the $\mathrm{P}=\mathrm{P}$ part at the $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX $(1.916+1.709=3.625$ for the in-plane $3 p, 1.584+1.195=$ 2.779 for $\left.3 p_{z}\right)$ are similar to those at $S_{1}$-geometry(90) (1.802× $2=3.604$ for the in-plane $3 p, 1.402 \times 2=2.804$ for $3 p_{z}$ ), respectively. This implies that the $3 p$ electron on the $\mathrm{P}^{\beta}$ relating to the smaller $\angle \mathrm{C}^{1^{\prime}} \mathrm{P}^{\beta} \mathrm{P}^{\alpha}$ angle $\beta$ transfers into the 3 p orbitals on the $\mathrm{P}^{\alpha}$ with the large $\angle \mathrm{C}^{1} \mathrm{P}^{\alpha} \mathrm{P}^{\beta}$ angle $\alpha$, which successfully escape from the electronic repulsion arising from the highly crowded local geometry around the $\mathrm{P}^{\beta}$ atom. The interpretation of the electron transfer from the $\mathrm{P}^{\beta}$ into the $\mathrm{P}^{\alpha}$ atom is valid at least for the case of the out-of-plane $3 p_{z}$ electron. However, we
do not interpret that the change of the in-plane $3 p$ electron population is due to the electron transfer from the $\mathrm{P}^{\beta}$ into the $\mathrm{P}^{\alpha}$ atom. The 3 s electron on the $\mathrm{P}^{\alpha}$ and $\mathrm{P}^{\beta}$ atoms exhibits a trend opposite to the case of the 3 p electron (i.e., decrease from 0.915 into 0.824 for the $\mathrm{P}^{\alpha}$ atom, increase from 0.915 into 0.996 for the $\mathrm{P}^{\beta}$ atom). Furthermore, the sum of the 3 s and in-plane $3 p$ electron on each atom at $S_{1} / S_{0}$-CIX (i.e., 2.740 for $P^{\alpha}, 2.705$ for $\mathrm{P}^{\beta}$ ) is not different from that at the $\mathrm{S}_{1}$-geometry $(90)$ (i.e., 2.717 for both the $\mathrm{P}^{\alpha}$ and $\mathrm{P}^{\beta}$ atoms), respectively. So we interpret the change of the in-plane 3 p electron population as follows. In the process of $S_{1}$-geometry $(90) \rightarrow S_{1} / S_{0}-C I X$, the electron on the $\mathrm{P}^{\beta}$ atom favors to be populated in a smaller space of the 3 s orbital rather than in a more spacious in-plane 3 p orbital because of a highly crowded geometry around the $\mathrm{P}^{\beta}$ atom, while the electron on the $\mathrm{P}^{\alpha}$ atom favors to be populated in a more spacious $3 p$ orbital because of a large $\angle \mathrm{C}^{1} \mathrm{P}^{\alpha} \mathrm{P}^{\beta}$ angle. In other words, the in-plane $3 p$ electron on the $\mathrm{P}^{\beta}$ atom is confined into the 3 s orbital, while that on the $\mathrm{P}^{\alpha}$ atom moves out from the 3 s orbital. That is, we interpret that the changes of the electron populations in the 3 s and the in-plane 3 p orbital are due to the rehybridization on each $\mathrm{P}^{\beta}$ and $\mathrm{P}^{\alpha}$ atom, not to the charge transfer from the $\mathrm{P}^{\beta}$ into the $\mathrm{P}^{\alpha}$ atoms. In conclusion, the highly distorted $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX is energetically stabilized in two ways: the out-of-plane $3 \mathrm{p}_{z}$ electron transfer from the $\mathrm{P}^{\beta}$ into the $\mathrm{P}^{\alpha}$ atom and the rehybridizations among the 3 s and in-plane 3 p electron on each P atom.

We confirm that such an electronic factor for the distorted $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX is not found in the symmetric inversion process of $S_{1}$-geometry $(90) \rightarrow S_{1} / S_{0}$-CIX(sym) which is energetically unfavorable. As seen in the relevant part of Table 4, the out-of-plane $3 p_{z}$ electron remains almost unchanged (from 1.402 to 1.382 ). The 3 s electron decreases from 0.915 to 0.744 , while the in-plane 3 p (i.e., $3 p_{x}+3 p_{y}$ ) electron increases from 1.802 into 2.196 . The change of the 3 s and the in-plane 3 p electron can be interpreted by the same reason for the case of the $\mathrm{P}^{\alpha}$ atom with the larger $\angle \mathrm{C}^{1} \mathrm{P}^{\alpha} \mathrm{P}^{\beta}$ angle in the nonsymmetric inversion route. In comparison with the electronic factor for the nonsymmetric inversion route, the following factors are missing in the symmetric inversion route: the $\pi$ electron transfer from the $\mathrm{P}^{\beta}$ onto the $\mathrm{P}^{\alpha}$ atom and the confinement of the inplane 3 p electron into the 3 s orbital on the $\mathrm{P}^{\beta}$ atom. In other words, these factors are important for the stabilization of the distorted $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX.

In turn we examine the electronic factors for the $S_{1}-S_{0}$ relaxation process of $A Z B$ under $N=N$ rotation-restricted condition. As mentioned in section 3.2., the symmetric inversion is energetically favorable. Table 5 lists the electron populations

TABLE 4: Electron Populations at Important Conformations of DPP

| geometry | $\mathrm{S}_{0}$ - geometry $^{\text {a }}$ |  | $\underline{\mathrm{S}_{1} \text {-geometry }(90)^{a}}$ | $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX | $\underline{\mathrm{S}_{1} / \mathrm{S}_{0}-\mathrm{CIX}(\mathrm{sym})}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| state | $\mathrm{S}_{0}$ | $\mathrm{S}_{1}$ | $\mathrm{S}_{1}$ | $\mathrm{S}_{1}$ | $\mathrm{S}_{1}$ |
| atomic orbitals on P |  |  |  |  |  |
| 3 s | 0.937 | 0.892 | 0.915 | $0.824(0.996)^{b}$ | 0.744 |
| $3 \mathrm{p}_{x}{ }^{\text {c }}$ | 0.837 | 0.857 | 0.866 | 0.920 (0.726) | 0.871 |
| $3 \mathrm{p}{ }^{\text {c }}$ | 1.279 | 0.926 | 0.936 | 0.996 (0.983) | 1.325 |
| in-plane $3 \mathrm{p}\left(3 \mathrm{p}_{x}+3 \mathrm{p}_{y}\right)^{c}$ | 2.116 | 1.784 | 1.802 | 1.916 (1.709) | 2.196 |
| $3 \mathrm{p}_{z}{ }^{\text {b }}$ | 0.994 | 1.397 | 1.402 | 1.584 (1.195) | 1.382 |
| net charge on P | 0.252 | 0.246 | 0.207 | 0.075 (0.375) | 0.103 |

${ }^{a}$ The values in columns of $\mathrm{S}_{0}$-geometry (for $\mathrm{S}_{0}$ and $\mathrm{S}_{1}$ ) and of $\mathrm{S}_{1}$-geometry $(90)$ (for $\mathrm{S}_{1}$ ) are different from those in columns of $\phi=30^{\circ}$ (for $\mathrm{S}_{0}$ and $\mathrm{S}_{1}$ ) and $\phi=90^{\circ}$ (for $\mathrm{S}_{1}$ ) in Table 5 of ref 8. The former are the values at $\mathrm{S}_{0}$-geometry and $\mathrm{S}_{1}$-geometry $(90)$ in Table 1 . On the other hand, the latter are the values at slightly different geometries. That is, the geometries in columns of $\phi=30^{\circ}$ and $\phi=90^{\circ}$ were obtained by setting to $\phi=30^{\circ}$ and $90^{\circ}$, where the other geometrical parameters are fixed to those of planar $\mathrm{S}_{0}$-geometry with $C_{2 h}$ (denoted by ( $\mathrm{S}_{0}$-geometry $\left(C_{2 h}\right)$ in ref 8 ). As commented in the footnote of Table 5 in ref 8 , this was to see the phenyl torsional angle dependence only. However, even in the present case of the fully optimized $\mathrm{S}_{0}$-geometry and $\mathrm{S}_{1}$-geometry( 90 ), a similar discussion can be done as in the text. ${ }^{b}$ Due to the asymmetric angles of $\alpha$ and $\beta$ at the $\mathrm{S}_{1} / \mathrm{S}_{0}-\mathrm{CIX}$, the electron population on the $\mathrm{P}^{\beta}$ atom in the parentheses is different from that on the $\mathrm{P}^{\alpha}$ atom. ${ }^{c}$ The directions of $x$-, $y$-, and $z$-axes are determined by diagonalizing the tensor of the moment of inertia. The $z$-axes for all the geometries are designed to be the out-of-plane $\pi$ orbitals over the $\mathrm{P}=\mathrm{P}$ bond, whereas the $x$ - and $y$-axes are the in-plane orbitals such as the nonbonding orbitals.
TABLE 5: Electron Populations at Important Conformations of AZB

| geometry | $\mathrm{S}_{0}$-geometry ${ }^{\text {a }}$ |  | $\underline{\mathrm{S}_{1} \text {-geometry }\left(C_{2 h}\right)}$ | $\underline{\mathrm{S}_{1} / \mathrm{S}_{0}-\mathrm{CIX}(\mathrm{sym})}$ | $\underline{\alpha}=180, \beta=78^{b}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| state | $\mathrm{S}_{0}$ | $\mathrm{S}_{1}$ | $\mathrm{S}_{1}$ | $\mathrm{S}_{1}$ | $\mathrm{S}_{1}$ |
| atomic orbitals on N |  |  |  |  |  |
| 2 s | 0.914 | 0.883 | 0.853 | 0.796 | 0.833 (1.040) ${ }^{\text {c }}$ |
| $2 \mathrm{p}_{x}{ }^{\text {d }}$ | 1.158 | 1.050 | 1.074 | 1.032 | 1.079 (0.958) |
| $2 \mathrm{p}_{y}{ }^{\text {d }}$ | 1.380 | 1.153 | 1.178 | 1.323 | 1.145 (1.174) |
| in-plane $2 \mathrm{p}\left(2 \mathrm{p}_{x}+2 \mathrm{p}_{y}\right)^{d}$ | 2.538 | 2.203 | 2.252 | 2.356 | 2.223 (2.132) |
| $2 \mathrm{p}{ }_{z}{ }^{\text {d }}$ | 0.996 | 1.370 | 1.350 | 1.321 | 1.502 (1.248) |
| net charge on N | -0.049 | -0.044 | -0.033 | -0.044 | -0.104 (-0.038) |

${ }^{a}$ The values are taken from ref $8 .{ }^{b}$ The geometry of $\alpha=180, \beta=78$ corresponds to the crossing point in Figure 6 b . ${ }^{c}$ Due to the asymmetric angles of $\alpha$ and $\beta$, the electron population on the $\mathrm{N}^{\beta}$ atom in the parentheses is different from that on the $\mathrm{N}^{\alpha}$ atom. ${ }^{d}$ The directions of $x$-, $y$-, and $z$-axes are determined by diagonalizing the tensor of the moment of inertia. The $z$-axes for all the geometries are designed to be the out-of-plane $\pi$ orbitals over the $\mathrm{N}=\mathrm{N}$ bond, whereas the $x$ - and $y$-axes are the in-plane orbitals such as the nonbonding orbitals.
at important conformations of AZB. In the process of $\mathrm{S}_{1}$ geometry $\left(C_{2 h}\right) \rightarrow \mathrm{S}_{1} / \mathrm{S}_{0}$-CIX(sym), the electron flow of the 2 s , in-plane 2 p (i.e., $2 \mathrm{p}_{x}+2 \mathrm{p}_{y}$ ), and out-of-plane $2 \mathrm{p}_{z}$ orbitals exhibits a trend similar to the case of the symmetric inversion of DPP. Nevertheless, the energy at the $S_{1} / S_{0}$-CIX(sym) of AZB $(2.81 \mathrm{eV})$ is much lower than that of $\operatorname{DPP}(6.50 \mathrm{eV})$. A clue for this difference is the net charges on the N and P atoms. In both cases, the N or P atoms becomes more negatively charged in the symmetric inversion process (from -0.033 to -0.044 for AZB in Table 5, from 0.207 to 0.103 for DPP in Table 4), which is ascribed to the electron transfer from the phenyl groups. In the case of $A Z B$, this electron transfer into the $\mathrm{N}=\mathrm{N}$ part is energetically favorable because the N atom is more electronegative than the $\mathrm{C}^{1}$ and $\mathrm{C}^{1^{\prime}}$ atoms. On the other hand, the electron transfer into the $\mathrm{P}=\mathrm{P}$ part is unfavorable in the case of DPP because of the more electropositive P atoms.

Before terminating the present paragraph, we summarize the electronic effects on the shapes of the PESs of DPP and AZB. In the case of AZB, the symmetric inversion is energetically favorable. This is because a large $\angle \mathrm{CNN}$ angle with $C_{2 h}$ symmetry serves the electron to flow into the more electronegative $\mathrm{N}=\mathrm{N}$ part so that the $\mathrm{S}_{1}$ state is not so destabilized even at large $\angle \mathrm{CNN}$ angles. In the case of DPP, the nonsymmetric inversion route is favorable. The $\mathrm{S}_{1} / \mathrm{S}_{0}$ - CIX takes a highly distorted geometry where one of the $\angle \mathrm{CPP}$ angles is large, while the other is enormously small. In order to stabilize the highly distorted $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX in $\mathrm{S}_{1}$, two types of the electronic reorganizations take place on the nonsymmetric inversion PES of $\mathrm{S}_{1^{-}}$ geometry $(90) \rightarrow \mathrm{S}_{1} / \mathrm{S}_{0}$-CIX. One is the $\pi$ electron transfer over
the $\mathrm{P}=\mathrm{P}$ bond so as to escape from the electronic repulsion at
 angle. The other is the rehybridizations of the 3 s and the inplane 3 p orbitals on each P atom. On the $\mathrm{P}^{\beta}$ atom with a small $\angle \mathrm{C}^{1^{\prime}} \mathrm{P}^{\beta} \mathrm{P}^{\alpha}$ angle, the electrons in the spacious in-plane 3 p orbitals are confined into the 3 s orbital. On the $\mathrm{P}^{\alpha}$ atom with a large $\angle \mathrm{C}^{1} \mathrm{P}^{\alpha} \mathrm{P}^{\beta}$ angle, the 3 s electron moves out to the more spacious 3 p orbitals. These rehybridizations are characteristic of the $\mathrm{P}=\mathrm{P}$ bond and not found in the $\mathrm{N}=\mathrm{N}$ bond of AZB (refer to the relevant part ( $\alpha=180, \beta=78$ ) in Table 5).
3.4. $S_{1}-S_{0}$ Relaxation Process of Realistic Diphosphene. In the previous subsections, we pointed out that the nonsymmetric inversion route of DPP is energetically favorable more than the symmetric inversion route for the $S_{1}-S_{0}$ relaxation in the $\mathrm{P}=\mathrm{P}$ rotation-restricted condition. In order to validate the discussion on the $S_{1}-S_{0}$ relaxation route of DPP, we performed additional calculations of a realistic diphosphene protected by a bulky 2,6-dimethylphenyl group more than phenyl group. Table 6 lists the characteristic optimized geometrical parameters of bis(2,6-dimethylphenyl)diphosphene (DMPDP). It is found that the two 2,6-dimethyphenyl groups of DMPDP are perpendicularly twisted against the $\mathrm{P}=\mathrm{P}$ bond even in $\mathrm{S}_{0}\left(\phi=\phi^{\prime}=\right.$ $91.8^{\circ}$ ), which is ascribed to a bulky substituent effect so as for DMPDP to escape from a steric repulsion with the $\mathrm{P}=\mathrm{P}$ part. This is in agreement with experimental and computational findings. ${ }^{33,34}$ In other words, DMPDP is a proper model for real diphosphenes. Furthermore, two following computational findings also validate that DMPDP is a proper model for the photochemistry of real diphosphenes to be discussed. The

TABLE 6: Characteristic Optimized Parameters at Important Conformations of DMPDP

| DMPDP | $\mathrm{S}_{0}$-geometry | $\mathrm{S}_{1}$-geometry |
| :--- | :---: | :---: |
|  | Bond Distances (angstroms) |  |
| $\mathrm{P}^{\alpha} \mathrm{P}^{\beta}$ | 2.051 | 2.146 |
| $\mathrm{P}^{\alpha} \mathrm{C}^{1}$ | 1.854 | 1.830 |
| $\mathrm{P}^{\beta} \mathrm{C}^{1^{\prime}}$ | 1.854 | 1.830 |
| Bond Angles (deg) |  |  |
| $\alpha\left(\mathrm{C}^{1} \mathrm{P}^{\alpha} \mathrm{P}^{\beta}\right)$ | 101.2 | 109.7 |
| $\beta\left(\mathrm{C}^{1^{\prime}} \mathrm{P}^{\beta} \mathrm{P}^{\alpha}\right)$ | 101.2 | 109.7 |
| Dihedral Angles $(\mathrm{deg})$ |  |  |
| $\tau\left(\mathrm{C}^{1} \mathrm{P}^{\alpha} \mathrm{P}^{\beta} \mathrm{C}^{1^{\prime}}\right)$ | 179.8 | 175.8 |
| $\phi\left(\mathrm{C}^{2} \mathrm{C}^{1} \mathrm{P}^{\alpha} \mathrm{P}^{\beta}\right)$ | 91.8 | 92.8 |
| $\phi^{\prime}\left(\mathrm{C}^{2^{\prime}} \mathrm{C}^{\left.1^{\prime} \mathrm{P}^{\beta} \mathrm{P}^{\alpha}\right)}\right.$ | 91.8 | 92.8 |

TABLE 7: Energies (eV) at Important Conformations of DMPDP

| DMPDP | $\mathrm{S}_{0}$-geometry | $\mathrm{S}_{1}$-geometry- <br> $(90)$ | $\mathrm{S}_{1} / \mathrm{S}_{0}-$ CIX $^{a}$ | $\mathrm{S}_{1} / \mathrm{S}_{0}-$ CIX- <br> $(\mathrm{sym})^{a}$ |
| :---: | :--- | :---: | :---: | :---: |
| $\mathrm{~S}_{0}$ | $0.0(0.0)^{b}$ |  | $4.710(3.789)$ | $6.866(6.147)$ |
| $\mathrm{S}_{1}$ | $3.232(2.605)$ | $2.938(2.428)$ | $4.793(3.848)$ | $7.081(6.025)$ |

${ }^{a}$ The geometrical parameters of the $\mathrm{S}_{1} / \mathrm{S}_{0}-\mathrm{CIX}$ and $\mathrm{S}_{1} /$ $\mathrm{S}_{0}$-CIX(sym) are commented on in the text. ${ }^{b}$ The numbers in the parentheses are the MRMP2 values.
excitation energies of DMPDP ( 2.605 eV in Table 7) well reproduce the experimental absorption maximum of 2.695 eV , $460 \mathrm{~nm} .{ }^{32}$ The $\mathrm{S}_{1}$-geometry $(90)$, which is similar to that of DPP, is not different from the $\mathrm{S}_{0}$-geometry (refer to Table 6). This rationalizes the experimental findings of the Raman excitation profile. ${ }^{35}$

The $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX and $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX(sym) of DMPDP were not fully optimized. Instead the geometrical parameters of the DPP parts of DMPDP were taken from those of DPP which were fully optimized (refer to Table 1). The geometrical parameters of the remaining methyl groups were taken from those of the $\mathrm{S}_{0^{-}}$ geometry of DMPDP because the geometrical parameters of the methyl groups at the $\mathrm{S}_{1}$-geometry $(90)$ are similar to those at the $\mathrm{S}_{0}$-geometry in Table 6. As seen in Table 7, the energy differences between $S_{1}$ and $S_{0}$ are kept small at the $S_{1} / S_{0}$-CIX and $S_{1} / S_{0}$-CIX(sym) of DMPDP. The energy at the $S_{1} / S_{0}$-CIX (ca. 3.85 eV ) is much lower than that at the $\mathrm{S}_{1} / \mathrm{S}_{0}-\mathrm{CIX}$ (sym) even in the case of DMPDP (ca. 6.03 eV ). This means that the nonsymmetric inversion route of DMPDP is energetically favorable more than the symmetric inversion route, as in the case of bare DPP.

On the basis of these computational findings, we make comment on the $\mathrm{S}_{1}-\mathrm{S}_{0}$ relaxation process of realistic diphosphenes protected by a bulky substituent in the $\mathrm{P}=\mathrm{P}$ rotationrestricted condition. One point is that this relaxation process is substantially the same as the second process of bare DPP discussed above. The only difference is that the first process where the phenyl groups are twisted from $30^{\circ}$ to $90^{\circ}$ is missing in the case of realistic diphosphenes such as DMPDP, because the bulky 2,6-dimethylphenyl groups are perpendicularly twisted against the $\mathrm{P}=\mathrm{P}$ part even in $\mathrm{S}_{0}$ due to a steric repulsion. Another point is that the energies at the $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIXs are higher by ca. 1.25 eV than those in $\mathrm{S}_{1}$ at $\mathrm{S}_{0}$-geometry irrespective of protection by bulky substituents or not (refer to Tables 3 and 7). This is much higher than the case of AZB (ca. 0.40 eV in Table 3). For the present, we have two interpretations for the high-energy location of the $S_{1} / S_{0}$-CIX since there are no experimental findings concerning the $\mathrm{S}_{1}-\mathrm{S}_{0}$ relaxation process in the $\mathrm{P}=\mathrm{P}$ rotation-restricted condition. One interpretation is that realistic
diphosphenes in $\mathrm{S}_{1}$ hardly decay into $\mathrm{S}_{0}$ and are more fluorescent than AZB in the $\mathrm{P}=\mathrm{P}$ or $\mathrm{N}=\mathrm{N}$ rotation-restricted condition. Another interpretation is that the $\mathrm{P}=\mathrm{P}$ rotation which is completely ignored in the present study plays an important role even in the $\mathrm{P}=\mathrm{P}$ rotation-restricted condition, as predicted by molecular dynamic simulation of $\mathrm{N}=\mathrm{N}$ rotation-restricted azobenzene derivatives of azobenzenophanes. ${ }^{30}$

## 4. Concluding Remarks

In the present paper we theoretically characterized the $\mathrm{P}=\mathrm{P}$ double bond from a viewpoint of the $S_{1}-S_{0}$ relaxation processes of DPP and realistic diphosphene in the $\mathrm{P}=\mathrm{P}$ rotation-restricted condition, in comparison with the $\mathrm{N}=\mathrm{N}$ double bond of AZB . In the case of DPP, the nonsymmetric inversion route where one of the two $\angle \mathrm{CPP}$ angles increases to a linear geometry of the CPP part is energetically favorable more than the symmetric inversion route where both the $\angle \mathrm{CPP}$ angles increase. This is contrastive with the case of AZB where the symmetric inversion is favorable. The difference of the $\mathrm{S}_{1}-\mathrm{S}_{0}$ relaxation PESs can be rationalized by two factors. One is the difference of the stable geometries in $\mathrm{S}_{1}$ around the Franck-Condon region. In the case of DPP, the phenyl groups are perpendicularly twisted due to the effective interaction between the nonbonding orbitals on the P atoms and the phenyl groups. In the case of AZB, on the other hand, the phenyl torsion is more impeded from a planar geometry due to the increase of the $\pi$ bond character in the linkage CN bond. The other is the flexibility of the $\mathrm{P}=\mathrm{P}$ double bond which allows DPP to take a highly distorted $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX with asymmetric $\angle \mathrm{CPP}$ angles. The $\pi$ electron over the $\mathrm{P}=\mathrm{P}$ bond becomes easily populated on the P atom relating to the larger $\angle \mathrm{CPP}$ angle in order to avoid the electronic repulsion between the $\mathrm{P}=\mathrm{P}$ part and the phenyl group relating to the smaller $\angle \mathrm{CPP}$ angle. The 3s and the in-plane 3p orbitals easily cause rehybridization. On the P atom relating to the smaller $\angle \mathrm{CPP}$ angle, the in-plane 3 p electron is confined into the smaller 3 s orbital, while the 3 s electron moves out to the more spacious 3 p orbitals on the other P atom in relation to the larger $\angle \mathrm{CPP}$ angle. This kind of rehybridization is not seen in the case of AZB with an $\mathrm{N}=\mathrm{N}$ bond.

Following our previous paper, ${ }^{8}$ we characterized the $\mathrm{P}=\mathrm{P}$ double bond from a viewpoint of the excited state in the present one. Thereby, we found that the PESs of diphosphenes for the $\mathrm{S}_{1}-\mathrm{S}_{0}$ relaxation process in the $\mathrm{P}=\mathrm{P}$ rotation-restricted condition are quite different from those of AZB. Our next concern is about the PESs for the $\mathrm{S}_{1}-\mathrm{S}_{0}$ relaxation of diphosphenes in the $\mathrm{P}=\mathrm{P}$ rotation-free condition. In the case of the $N=N$ rotation-free condition of AZB, the $N=N$ rotation easily takes place so as for AZB to directly reach an $\mathrm{S}_{1} / \mathrm{S}_{0}$-CIX at the dihedral angle $\angle C N N C \sim 90^{\circ} .{ }^{25-29}$ Furthermore, it is pointed out that the $S_{1}-S_{0}$ relaxation via the $\mathrm{N}=\mathrm{N}$ rotation can take place even in the case of the azobenzenophanes where the $\mathrm{N}=\mathrm{N}$ rotation is thought to be blocked. ${ }^{30}$ So we checked if realistic diphosphene protected by a bulky substituent (i.e., bis(2,4,6-tri-tert-butylphenyl)diphosphene) reaches a perpendicularly twisted (i.e., the dihedral angle $\angle \mathrm{CPPC} \sim 90^{\circ}$ ) conformation by a simple $\mathrm{P}=\mathrm{P}$ twist of the molecular model in hand. A simple twist of the $\mathrm{P}=\mathrm{P}$ bond of this realistic diphosphene causes an unfavorable contact between the tert-butyl groups, whereas that of unrealistic DPP without any bulky substituent does not. On the basis of a speculation with the molecular model, we imagine a story different from the case of AZB. That is, realistic diphosphenes reach an $S_{1} /$ $\mathrm{S}_{0}$-CIX at the dihedral angle $\angle \mathrm{CPPC} \sim 90^{\circ}$ not via a direct $\mathrm{P}=\mathrm{P}$ rotation but via an indirect route, even if possible. We are now in progress of the scanning of the PESs relating to the $\mathrm{S}_{1}-\mathrm{S}_{0}$ relaxation route under $\mathrm{P}=\mathrm{P}$ rotation-free condition.

Acknowledgment. This work is financially supported by Grant-in-Aid for Priority Area (Molecular Theory for Real Systems) (Nos. 19029004 and 20038004) from the Ministry of Education, Culture, Sports, Science and Technology.

## References and Notes

(1) Weber, L. Chem. Rev. 1992, 92, 1839-1906.
(2) Power, P. P. Chem. Rev. 1999, 99, 3463-3503.
(3) Mathey, F. Angew. Chem., Int. Ed. 2003, 42, 1578-1603.
(4) Wright, V. A.; Gates, D. P. Angew. Chem., Int. Ed. 2002, 41, 23892392.
(5) Smith, R. C.; Protasiewicz, J. D. J. Am. Chem. Soc. 2004, 126, 2268-2269.
(6) Kawasaki, S.; Nakamura, A.; Toyota, K.; Yoshifuji, M. Bull. Chem. Soc. Jpn. 2005, 78, 1110-1120.
(7) Cowley, A. H.; Decken, A.; Norman, N. C.; Krüger, C.; Lutz, F.; Jacobsen, H.; Ziegler, T. J. Am. Chem. Soc. 1997, 119, 3389-3390.
(8) Amatatsu, Y. J. Phys. Chem. A 2008, 112, 8824-8828.
(9) Botolus, P.; Monti, S. J. Phys. Chem. 1979, 83, 648-652.
(10) Rau, H.; Lüddecke, E. J. Am. Chem. Soc. 1982, 104, 1616-1620.
(11) Wachtveitl, J.; Nägele, T.; Puell, B.; Zinth, W.; Krüger, M.; Rudolph-Böhner, S.; Oesterhelt, D.; Moroder, L. J. Photochem. Photobiol., A 1997, 105, 283-288.
(12) Nägele, T.; Hoche, R.; Zinth, W.; Wachtveitl, J. Chem. Phys. Lett. 1997, 272, 489-495.
(13) Lednev, I. K.; Ye, T.-Q.; Matousek, P.; Towrie, M.; Foggi, P.; Neuwahl, F. V. R.; Umapathy, S.; Hester, R. E.; Moore, J. N. Chem. Phys. Lett. 1998, 290, 68-74.
(14) Lednev, I. K.; Ye, T.-Q.; Abbott, L. C.; Hester, R. E.; Moore, J. N. J. Phys. Chem. A 1998, 102, 9161-9166.
(15) Fujino, T.; Tahara, T. J. Phys. Chem. A 2000, 104, 4203-4210.
(16) Fujino, T.; Arzhantsef, S. Y.; Tahara, T. J. Phys. Chem. A 2001, 105, 8123-8129.
(17) Hirose, Y.; Yui, H.; Sawada, T. J. Phys. Chem. A 2002, 106, 30673071.
(18) Satzger, H.; Spörlein, S.; Root, C.; Wachtveitl, J.; Zinth, W.; Gilch, P. Chem. Phys. Lett. 2003, 372, 216-223.
(19) Satzger, H.; Root, C.; Braun, M. J. Phys. Chem. A 2004, 108, 62656271.
(20) Schmidt, B.; Sobotta, C.; Mulkmas, S.; Laimgruber, S.; Braun, M.; Zinth, W.; Gilch, P. J. Phys. Chem. A 2004, 108, 4399-4404.
(21) Chang, C.-W.; Lu, Y.-C.; Wang, T.-T.; Diau, E. W.-G. J. Am. Chem. Soc. 2004, 126, 10109-10118.
(22) Lu, W.-C.; Diau, E. W.-G.; Rau, H. J. Phys. Chem. A 2005, 109, 2090-2099.
(23) Pancur, T.; Renth, F.; Temps, F.; Harbaum, B.; Krüger, A.; Herges, R.; Näther, Chr. Phys. Chem. Chem. Phys. 2005, 7, 1985-1989.
(24) Poprawa-Smoluch, M.; Baggerman, J.; Zhang, H.; Maas, H. P. A.; De Cola, L.; Brouwer, A. M. J. Phys. Chem. A 2006, 110, 11926-11937. (25) Ishikawa, T.; Noro, T.; Shoda, T. J. Chem. Phys. 2002, 115, 75037512.
(26) Diau, E. W.-G. J. Phys. Chem. A 2004, 108, 950-956.
(27) Cembran, A.; Bemardi, F.; Garavelli, M.; Gagliardi, L.; Orlandi, G. J. Am. Chem. Soc. 2004, 126, 3234-3243.
(28) Tiago, M. L.; Ismail-Beigi, S.; Louie, S. G. J. Chem. Phys. 2005, 122, 094311/1-7.
(29) Crecca, C. R.; Roitberg, A. E. J. Phys. Chem. A 2006, 110, 81888203.
(30) Ciminelli, C.; Granucci, G.; Persico, M. J. Chem. Phys. 2005, 123, 174317/1-10.
(31) Schmidt, M. W.; Baldridge, K. K.; Boatz, J. A.; Elbert, S. T.; Gordon, M. S.; Jensen, J. H.; Koseki, S.; Matsunaga, N.; Nguyen, K. A.; Su, S. J.; Windus, T. L.; Dupuis, M.; Montgomery, J. A., Jr. J. Comput. Chem. 1993, 14, 1347-1363.
(32) Frisch, M. J.; Trucks, G. W.; Schlegel, H. B.; Scuseria, G. E.; Robb, M. A.; Cheeseman, J. R.; Montgomery, J. A., Jr.; Vreven, T.; Kudin, K. N.; Burant, J. C.; Millam, J. M.; Iyengar, S. S.; Tomasi, J. J.; Barone, V.; Mennucci, B.; Cossi, M.; Scalmani, G.; Rega, N.; Petersson, G. A.; Nakatsuji, H.; Hada, M.; Ehara, M.; Toyota, K.; Fukuda, R.; Hasegawa, J.; Ishida, M.; Nakajima, T.; Honda, Y.; Kitao, O.; Nakai, H.; Klene, M.; Li, X.; Knox, J. E.; Hratchian, H. P.; Cross, J. B.; Adamo, C.; Jaramillo, J.; Gomperts, R.; Stratmann, R. E.; Yazyev, O.; Austin, A. J.; Cammi, R.; Pomelli, C.; Ochterski, J. W.; Ayala, P. Y.; Morokuma, K.; Voth, A.; Salvador, P.; Dannenberg, J. J.; Zakrzewski, V. G.; Dapprich, S.; Daniels, A. D.; Strain, M. C.; Farkas, O.; Malick, D. K.; Rabuck, A. D.; Raghavachari, K.; Foresman, J. B.; Ortiz, J. V.; Cui, Q.; Baboul, A. G.; Clifford, S.; Cioslowski, J.; Stefanov, B. B.; Liu, G.; Liashenko, A.; Piskorz, P.; Komaromi, I.; Martin, R. L.; Fox, D. J.; Keith, T.; Al-Laham, M. A.; Peng, C. Y.; Nanayakkara, A.; Challacombe, M.; Gill, P. M. W.; Johnson, B.; Chen, W.; Wong, M. W.; Gonzalez, C.; Pople, J. A. Gaussian 03, revision B.04; Gaussian, Inc.: Pittsburgh, PA, 2003.
(33) Hamaguchi, H.; Tasumi, M.; Yoshifuji, M.; Inamoto, N. J. Am. Chem. Soc. 1984, 106, 508-509.
(34) Sasamori, T.; Takeda, N.; Tokitoh, N. J. Phys. Org. Chem. 2003, 16, 450-462.
(35) Copeland, T.; Shea, M. P.; Milliken, M. C.; Smith, R. C.; Protasiewicz, J. D.; Simpson, M. C. Anal. Chim. Acta 2003, 496, 155-163.

[^1]
[^0]:    $\dagger$ E-mail: amatatsu@ipc.akita-u.ac.jp. Fax: 81-18-889-2601.

[^1]:    JP902217H

